# $\mathcal{G}$-Mixup: Graph Data Augmentation for Graph Classification 

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## Overview

(1) Background and Motivation
(2) Methodology

- $\mathcal{G}$-Mixup
- Implementation
(3) Experiments
- Verification Experiments
- Performance Experiments


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## Mixup

Mixup is a cross-instance data augmentation method, which linearly interpolates random sample pair to generate more synthetic training data.

$$
\begin{aligned}
& \mathbf{x}_{\text {new }}=\lambda \mathbf{x}_{i}+(1-\lambda) \mathbf{x}_{j}, \\
& \mathbf{y}_{\text {new }}=\lambda \mathbf{y}_{i}+(1-\lambda) \mathbf{y}_{j}
\end{aligned}
$$


where $\left(\mathbf{x}_{i}, \mathbf{y}_{i}\right),\left(\mathbf{x}_{j}, \mathbf{y}_{j}\right)$ are two samples randomly drawn from training data.
Mixup have been empirically and theoretically shown to improve the generalization and robustness of deep neural networks (H. Zhang et al., 2017; L. Zhang et al., 2021).

Can we mix up input graph pair to improve graph neural networks?

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- Image is in Euclidean space

(1) Graph data is irregular (the number of nodes)
(2) Graph data is not well-aligned (nodes not naturally ordered)
(3) Graph has divergent topology information
- Graph is in non-Euclidean space


## Graph Generator: Graphon

The real-world graphs can be regarded as generated from generator (i.e., graphon ${ }^{1}$ ). For example,


The graphons of different graphs are regular, well-aligned, and in Euclidean space.

We propose to mix up graph generator (i.e., graphon) to achieve the input graph mixup.

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## $\mathcal{G}$-Mixup

We propose to mixup the generator (i.e., graphon) of graphs, mix up the graphons of different classes, and then generate synthetic graphs.


The formal mathematical expression are as follows:
(1) Graphon Estimation:

$$
\mathcal{G} \rightarrow W_{\mathcal{G}}, \mathcal{H} \rightarrow W_{\mathcal{H}}
$$

(2) Graphon Mixup:

$$
W_{\mathcal{I}}=\lambda W_{\mathcal{G}}+(1-\lambda) W_{\mathcal{H}}
$$

(3) Graph Generation: $\quad\left\{I_{1}, I_{2}, \cdots, I_{m}\right\} \stackrel{\text { i.i.d }}{\sim} \mathbb{G}\left(K, W_{\mathcal{I}}\right)$
(4) Label Mixup: $\quad \mathbf{y}_{\mathcal{I}}=\lambda \mathbf{y}_{\mathcal{G}}+(1-\lambda) \mathbf{y}_{\mathcal{H}}$

## Implementation


(1) Graphon Estimation. We use the step function (Lovász, 2012; Xu et al., 2021) to approximate graphons. In general, the step function can be seen as a matrix $\mathbf{W}=\left[w_{k k^{\prime}}\right] \in[0,1]^{K \times K}$, where $\mathbf{W}_{i j}$ is the probability that an edge exists between node $i$ and node $j$.
(2) Synthetic Graphs Generation. Generates an adjacency matrix $\boldsymbol{A}=\left[a_{i j}\right] \in\{0,1\}^{K \times K}$, whose element values follow the Bernoulli distributions $(\cdot)$ determined by the step function.

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## Do different classes of graphs have different graphons?

We visualize the estimated graphons on IMDB-BINARY, REDDIT-BINARY, and IMDB-MULTI.


IMDB-BINARY


REDDIT-BINARY


IMDB-MULTI

We make the following observations:
(1) Real-world graphs of different classes have different graphons.
(2) This observation lays a solid foundation for our proposed method.

## What is $\mathcal{G}$-Mixup doing? A case study

We visualize the generated synthetic graphs on REDDIT-BINARY dataset.


We make the following observations:
(1) The class 0 has one high-degree node while class 1 have two (a)(b).
(2) The generated graphs based on

- $\left(1 * W_{0}+0 * W_{1}\right)$ have one high-degree node (c).
- $\left(0 * W_{0}+1 * W_{1}\right)$ have two high-degree nodes (d).
- $\left(0.5 * W_{0}+0.5 * W_{1}\right)$ have a high-degree node and a dense subgraph (e).
(3) Graphs generated by $\mathcal{G}$-Mixup are the mixture of original graphs.


## Can $\mathcal{G}$-Mixup improve the performance of GNNs?

We use different GNNs for graph classification and report the performance comparisons of $\mathcal{G}$-Mixup.

| Dataset | IMDB-B | IMDB-M | REDD-B | REDD-M5 | REDD-M12 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| \#graphs | 1000 | 1500 | 2000 | 4999 | 11929 |
| \#classes | 2 | 3 | 2 | 5 | 11 |
| \#avg.nodes | 19.77 | 13.00 | 429.63 | 508.52 | 391.41 |
| \#avg.edges | 96.53 | 65.94 | 497.75 | 594.87 | 456.89 |
| vanilla | 72.18 | 48.79 | 78.82 | 45.07 | 46.90 |
| U w/ Dropedge | 72.50 | 49.08 | 81.25 | 51.35 | 47.08 |
| w/ DropNode | 72.00 | 48.58 | 79.25 | 49.35 | 47.93 |
| w/ Subgraph | 68.50 | 49.58 | 74.33 | 48.70 | 47.49 |
| w/ M-Mixup | 72.83 | 49.50 | 75.75 | 49.82 | 46.92 |
| w/ G-Mixup | $\mathbf{7 2 . 8 7}$ | $\mathbf{5 1 . 3 0}$ | $\mathbf{8 9 . 8 1}$ | $\mathbf{5 1 . 5 1}$ | $\mathbf{4 8 . 0 6}$ |
| vanilla | 71.55 | 48.83 | 92.59 | 55.19 | 50.23 |
| ㄴ w/ Dropedge | $\mathbf{7 2 . 2 0}$ | 48.83 | 92.00 | 55.10 | 49.77 |
| w/ DropNode | 72.16 | 48.33 | 90.25 | 53.26 | 49.95 |
| w/ Subgraph | 68.50 | 47.25 | 90.33 | 54.60 | 49.67 |
| w/ M-Mixup | 70.83 | 49.88 | 90.75 | 54.95 | 49.81 |
| w/ G-Mixup | 71.94 | $\mathbf{5 0 . 4 6}$ | $\mathbf{9 2 . 9 0}$ | $\mathbf{5 5 . 4 9}$ | $\mathbf{5 0 . 5 0}$ |


| Method | IMDB-B | IMDB-M | REDD-B | REDD-M5k |
| :---: | :---: | :---: | :---: | :---: |
| $\bar{\circ}$ vanilla | 72.37 | 50.57 | 90.30 | 45.07 |
| w/ Dropedge | 71.75 | 48.75 | 88.96 | 47.43 |
| 등 w/ DropNode | 69.16 | 48.50 | 81.33 | 46.15 |
| $\stackrel{\circ}{ }$ w/ Subgraph | 67.83 | 50.83 | 86.08 | 45.75 |
| w/ M-Mixup | 71.83 | 51.22 | 87.58 | 45.60 |
| w/ $\mathcal{G}$-Mixup | 72.80 | 51.30 | 90.40 | 46.48 |
| $\bar{\circ}$ vanilla | 71.68 | 47.75 | 78.40 | 31.61 |
| ¢ w/ Dropedge | 69.16 | 49.44 | 76.00 | 34.46 |
| - w/ DropNode | 70.25 | 46.83 | 76.68 | 33.10 |
| w/ Subgraph | 69.50 | 46.00 | 76.06 | 31.65 |
| w/ M-Mixup | 66.50 | 45.16 | 78.37 | 34.46 |
| w/ $\mathcal{G}$-Mixup | 73.25 | 50.70 | 78.87 | 38.42 |
| $\bar{\circ}$ vanilla | 73.25 | 49.04 | 84.95 | 49.32 |
| $\bigcirc$ | 69.16 | 49.66 | 81.37 | 47.20 |
| 3 w/ DropNode | 73.50 | 49.91 | 85.68 | 46.82 |
| . $\sum^{\text {w/ }}$ Subgraph | 70.25 | 48.18 | 84.91 | 49.22 |
| $\sum$ w/ M-Mixup | 70.62 | 49.96 | 85.12 | 47.20 |
| w/ $\mathcal{G}$-Mixup | 73.93 | 50.29 | 85.87 | 50.12 |

## We make the following observation:

(1) $\mathcal{G}$-Mixup can improve the performance of GNNs on various datasets.

## Can $\mathcal{G}$-Mixup improve the performance of GNNs?

We present the training/validation/test curves on IMDB-BINARY, IMDB-MULTI, REDDIT-BINARY and REDDIT-MULTI-5K with GCN.



REDDIT-BINARY


REDDIT-MULTI-5K


We make the following observations:
(1) The loss curves of $\mathcal{G}$-Mixup are lower than the vanilla model.
(2) $\mathcal{G}$-Mixup can improve the generalization of graph neural networks.

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## $\mathcal{G}$-Mixup: Graph Data Augmentation for Graph Classification

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## Q\&A




[^0]:    ${ }^{1}$ For ease of exposition, we use step function as grpahon in the following.

